

On the Concept of “Dynamic (In)Stability of Quasi-Static Paths”

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A concept of dynamic stability of quasi-static paths is proposed that takes into account the existence of fast (dynamic) and slow (quasi-static) time scales. A change of variables is performed that replaces the (fast) physical time t by a (slow) loading parameter λ , whose rate of change with respect to time, $\varepsilon = d\lambda/dt$, is decreased to zero. This leads to a system of dynamic equations defining a singular perturbation problem: the highest order derivative with respect to λ appears multiplied by ε . The proposed definition is essentially a continuity property with respect to the smallness of initial perturbations (as in Lyapunov stability) and loading rate ε (as in singular perturbation problems). Three mechanical examples (the Ziegler and Shanley columns and a pin-on-flat friction apparatus) are presented to illustrate similarities and differences between “dynamic stability of quasi-static paths” and Lyapunov stability of some related equilibrium configurations or dynamic trajectories.

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