

**CONEX Program**  
**COOPERATION AND NETWORKING FOR EXCELLENCE**

**Project Title:**  
**Emulsions with Nanoparticles for New Materials**

**Short Project Title: EMMA**

**Partners:**

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## Nano-structured materials – “hot topic” in the materials science:

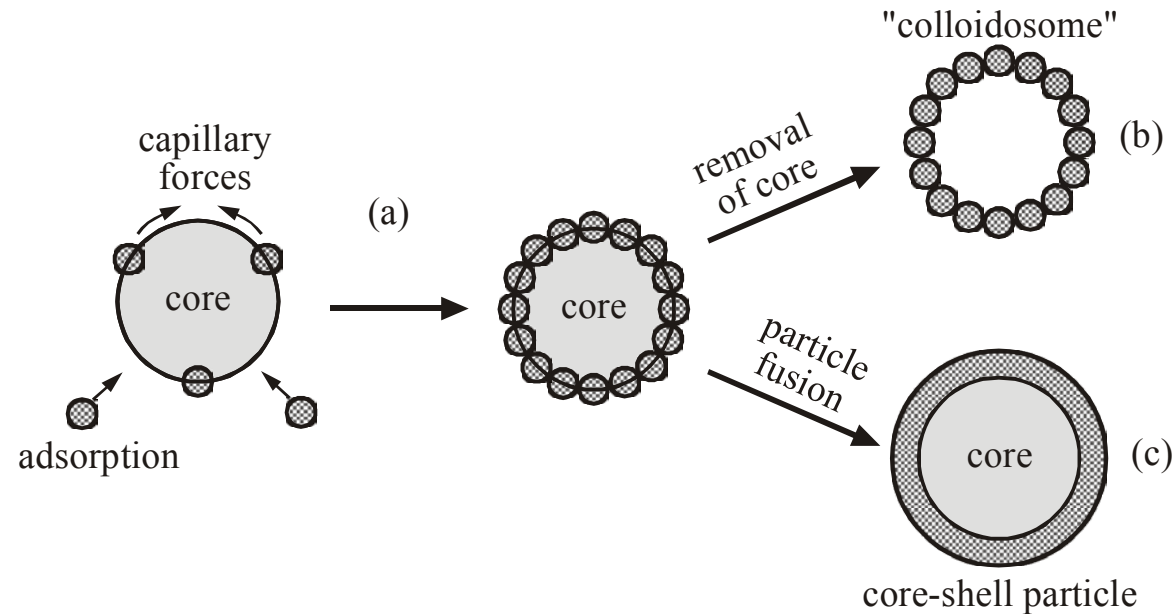
- nanostructured surfaces for photoelectrochemical and photocathalytic processes;
- paint coatings of new optical properties;
- structured nanoporous materials using colloid crystal templates;
- preparation of core-shell colloid particles of various structures and compositions;
- micro-capsules for encapsulation of drugs, enzymes, minerals, dyes, phase-change materials;
- micro-reaction cages.

## The main purpose of the project:

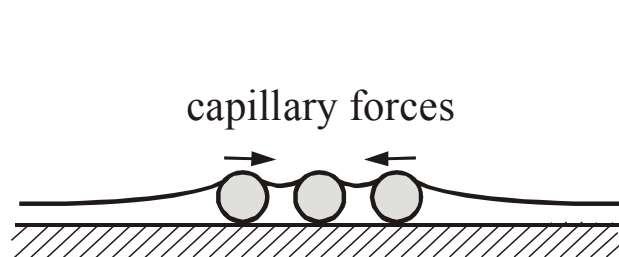
Use of emulsions stabilized by solid particles

for fabrication of nano-composites (colloidosomes, microcapsules, core-shell and composite particles), nano-structured surfaces and porous layers

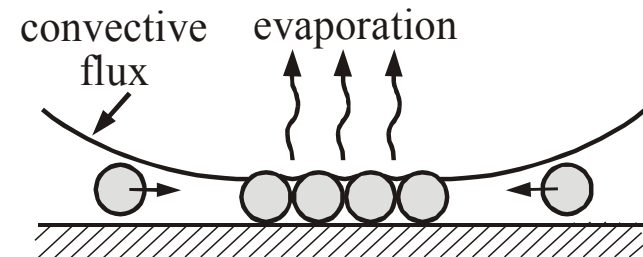
by using emulsion droplets as precursors and/or templates



(a) Particle assembly on emulsion drops to produce (b) “colloidosome” or (c) “core-shell” particles



(d) Nucleus formation by capillary forces



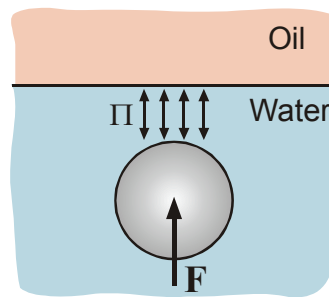
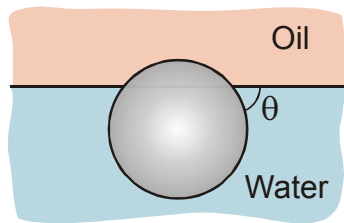
(e) 2D crystal growth due to evaporation driven convective flux

Formation of particulate layers from colloid particles (including colloidosomes and core-shell particles) by the method of **convective self-assembly**.

# Formation of Pickering Emulsions (Emulsions Stabilized by Solid Particles)

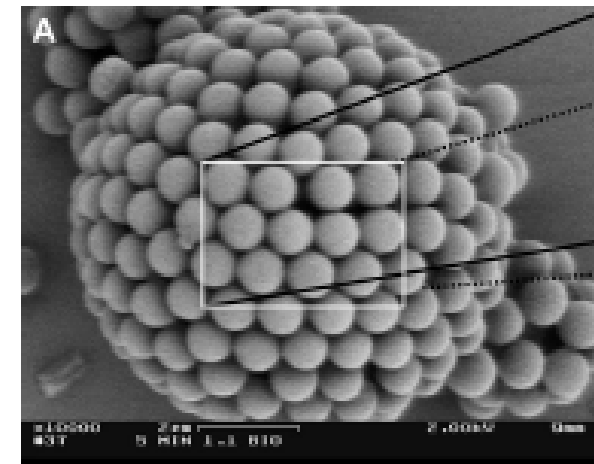
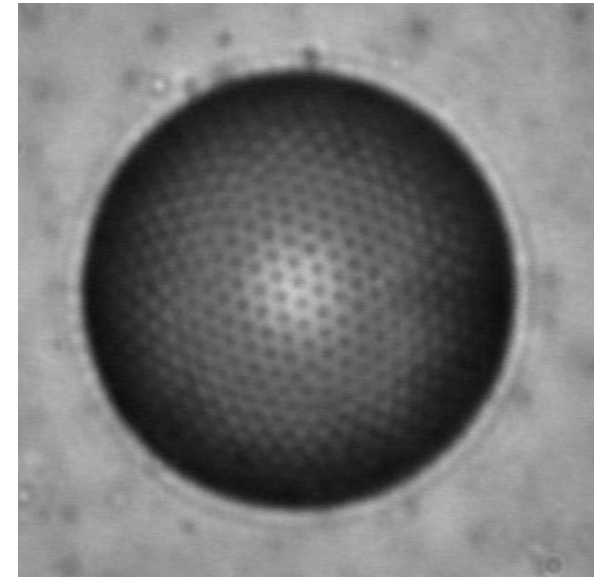
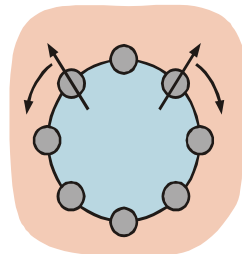
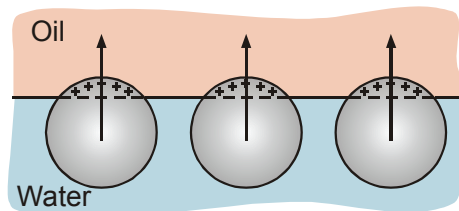
⇒ The solid particles form a shell protecting the emulsion drops against coalescence;

⇒ The adsorption energy of the particles is very high, but they could encounter a barrier to adsorption;



$$W_{ads} = \pi R_p^2 \sigma_{ow} (1 - \cos\theta)^2 \gg kT$$

⇒ A balance of **electrostatic repulsion** and **capillary attraction** lead to particle packing and ordering.



## Kinds of Capillary Forces between Particles:

### Lateral Capillary Forces:

$$F = -2\pi\sigma Q_1 Q_2 q K_1(qL)$$

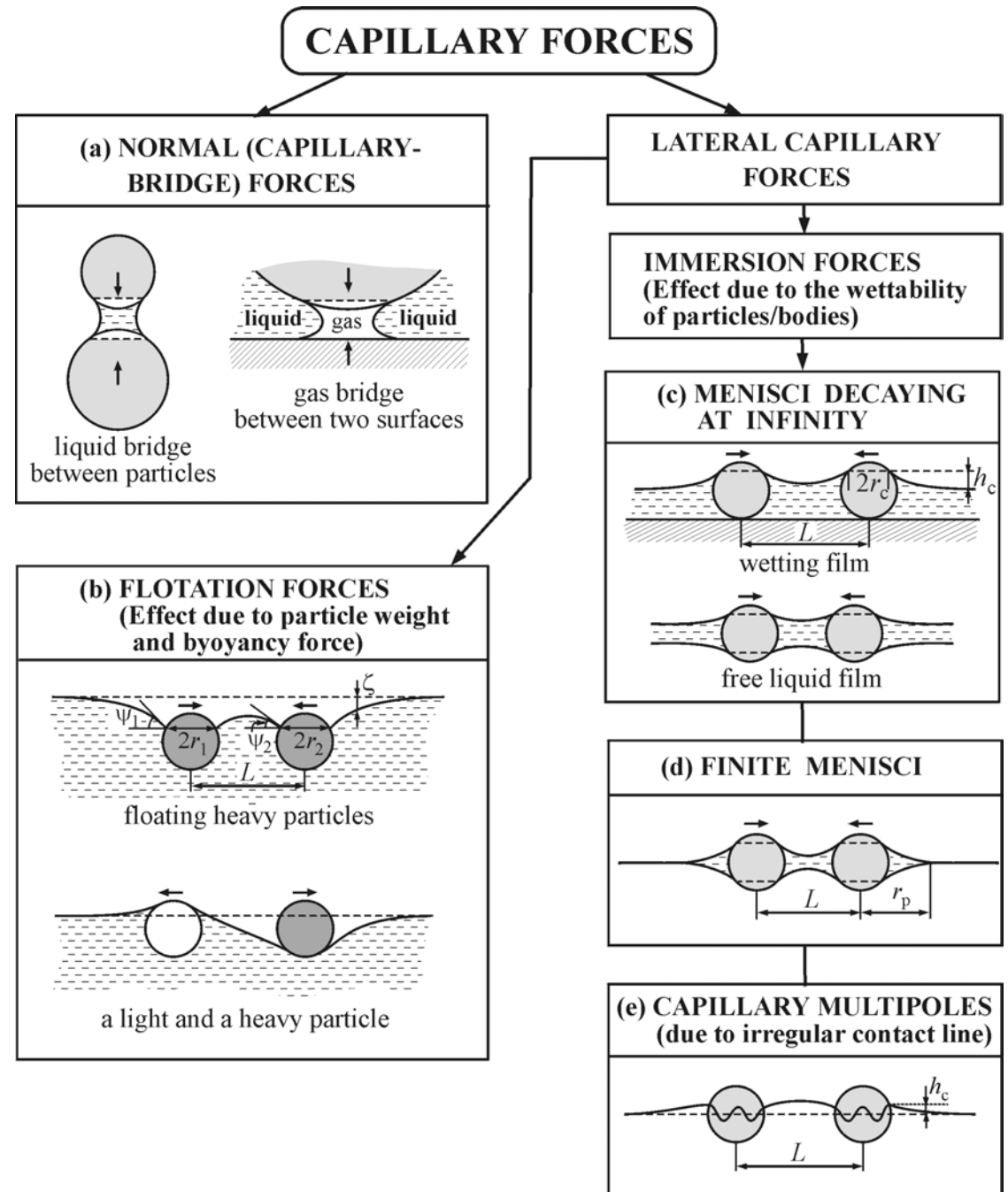
$$F = -2\pi\sigma \frac{Q_1 Q_2}{L} \quad \text{for } r_k \ll L \ll q^{-1}$$

(2D analogue of the Coulomb law in electrostatics)

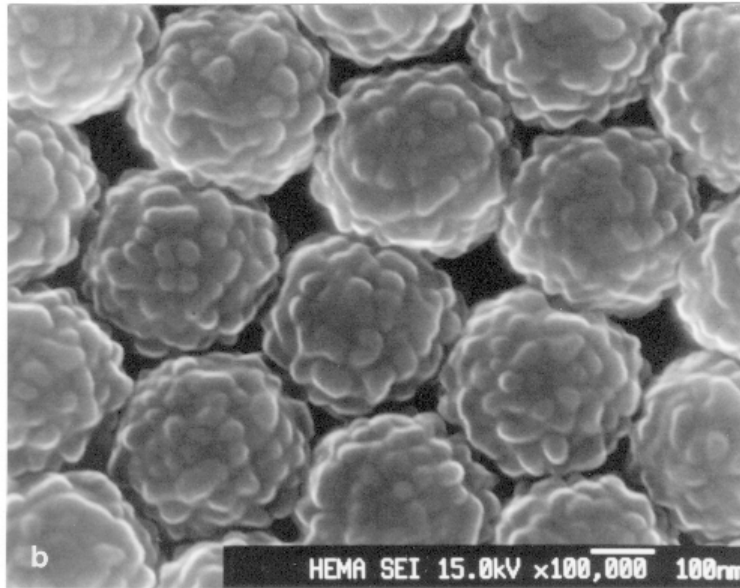
$$Q_k = r_k \sin \psi_k = \frac{F_N^{(k)}}{2\pi\sigma} \quad (k = 1, 2)$$

– “Capillary Charge”

(characterises the interfacial deformation caused by the respective particle)



## New Aspects of Capillary Forces:



### (1) Interaction between Capillary Multipoles

(the particles in Pickering emulsions are often rough-edged)

Meniscus around particles of undulated contact line:

$$\zeta(r, \varphi) = \sum_{m=0}^{\infty} K_m(qr) (A_m \cos m\varphi + B_m \sin m\varphi)$$

Analogy with electrostatics:

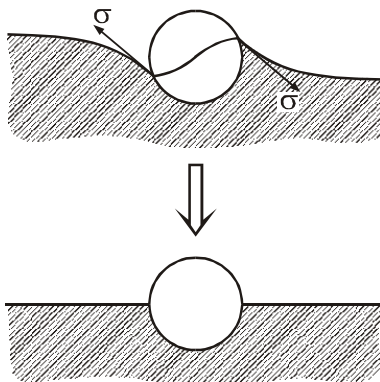
$m = 0$  – “capillary charges”

$m = 1$  – “capillary dipoles”

$m = 2$  – “capillary quadrupoles”

$m = 3$  – “capillary hexapoles”

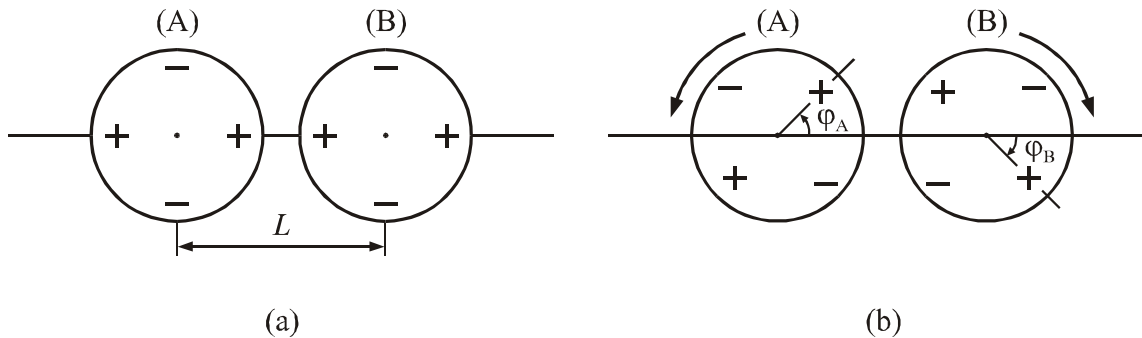
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The capillary force spontaneously rotates a floating particle to annihilate its dipole moment ( $m = 1$ )

⇒ The leading multipole orders are the charges and quadrupoles.

## Interaction between “Capillary Quadrupoles”



The signs “+” and “-” symbolize convex and concave local deviations of the contact line from planarity.

(a) Initial state. (b) After rotation of the respective particles at angles  $\varphi_A$  and  $\varphi_B = -\varphi_A$ .

$$\Delta W(L) = -12\pi\sigma H^2 \cos(2\varphi_A + 2\varphi_B) \frac{r_c^4}{L^4}, \quad (m = 2; L \gg 2r_c)$$

Particles in contact ( $L/r_c = 2$ ); optimal orientation,  $\cos(2\varphi_A + 2\varphi_B) = 1$ :

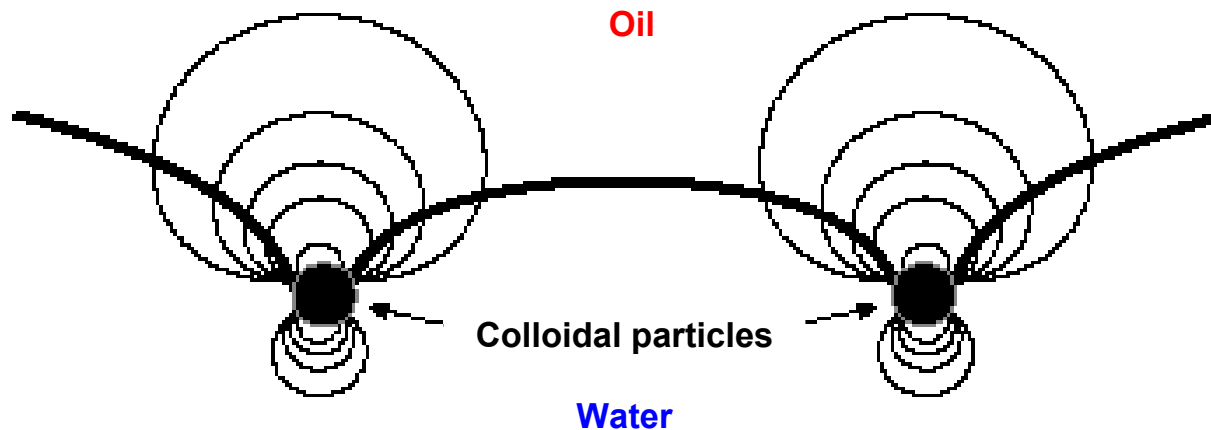
$$\Delta W = - (3/4)\pi\sigma H^2$$

For  $\sigma = 35$  mN/m:  $\Delta W$  becomes greater than the thermal energy  $kT$  for undulation amplitude  $H > 2.2$  Å.

⇒ Even a minimal roughness of the contact line could be sufficient to give rise to a significant capillary attraction, which may produce 2D aggregation of the colloidal particles.

**New Task:** Derive general expressions for all types of capillary multipoles; rheology of particle monolayers

## New Aspects: (2) Electric-Field Induced Capillary Forces



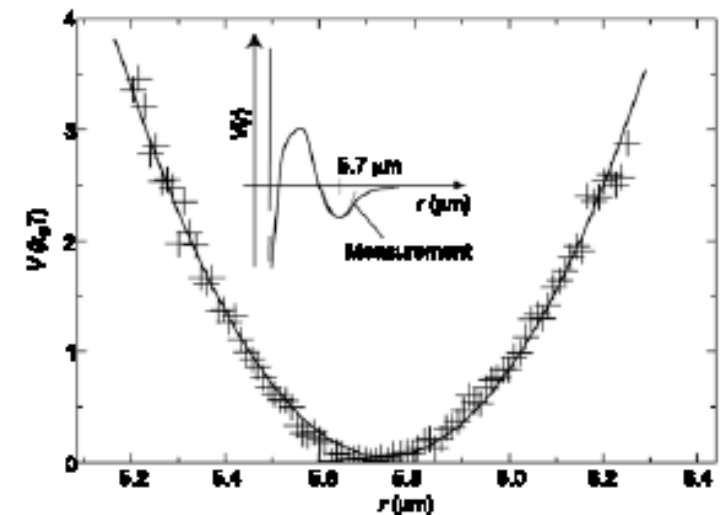
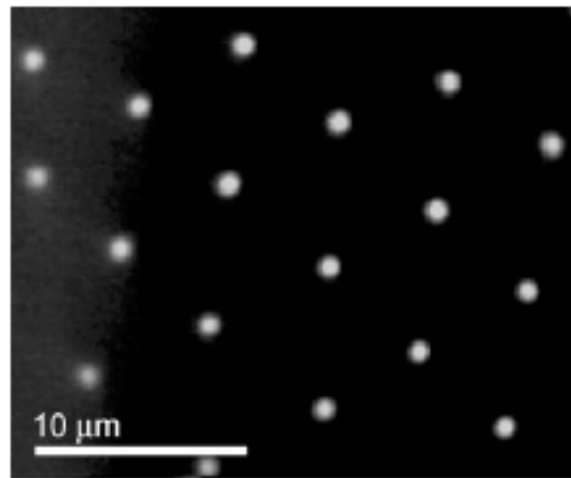
The electric force pushes each particle toward the water phase.

The overlap of the interfacial distortions around the two particles leads to a strong lateral capillary attraction.

D. Weitz et al. Nature (2002): A rather universal effect, appears with particles from nm to mm size!

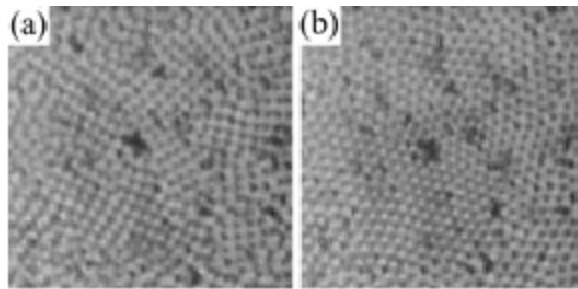
New Task: Develop a rigorous theory of:

- (1) electro-dipping force;
- (2) lateral capillary and electric force

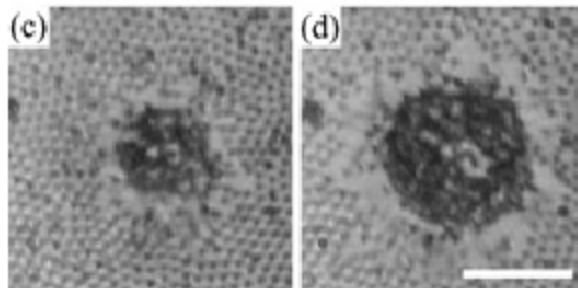




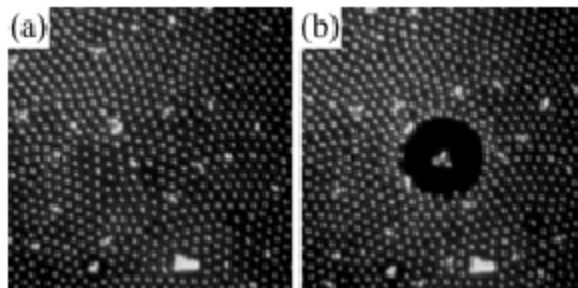
## New Aspects: (3) Particles at Meniscus of Non-uniform Curvature



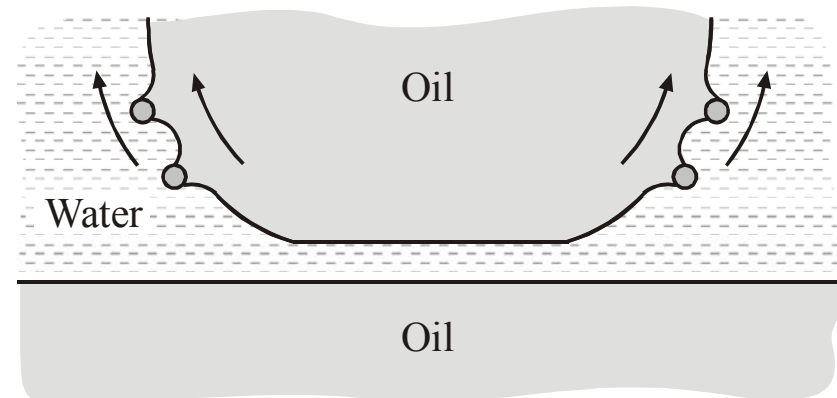
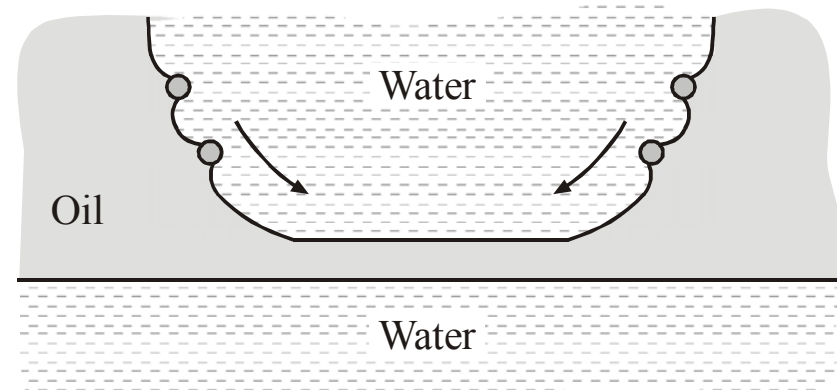
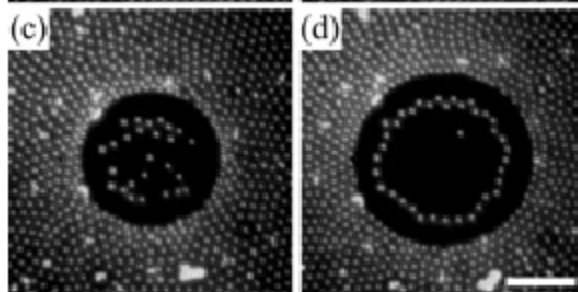
Water  
in  
Oil



(Fuller et al.)



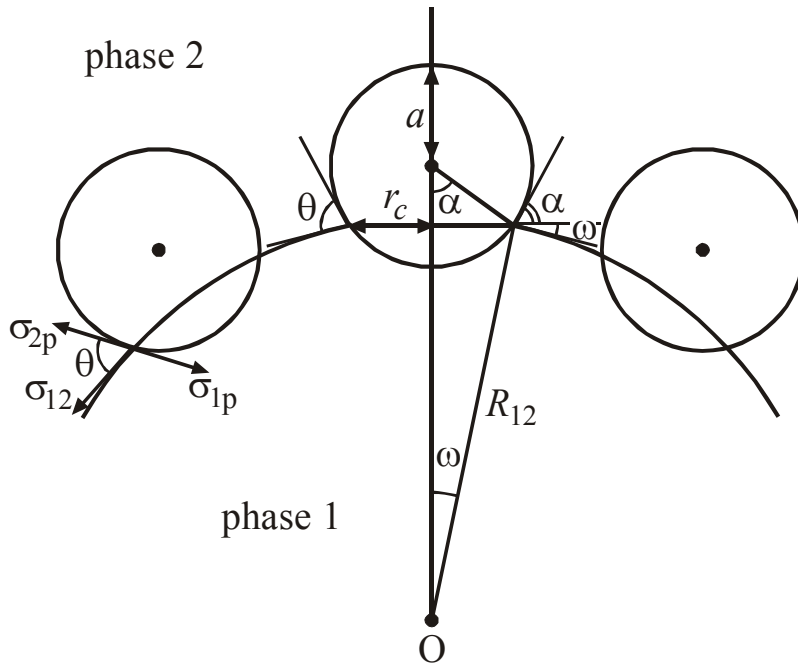
Oil  
in  
Water



Possible explanation: The particles can be (1) **attracted** or (2) **repelled** from the flat zone. **Electro-dipping force** operative.

**Task:** Investigate this effect

## Thermodynamic Aspects of Production of Pickering Emulsions



### Interfacial Work of Emulsification:

$$W = \sigma_{12} A_{12} + \sigma_{1p} A_{1p} + \sigma_{2p} A_{2p} + N_b \sigma_{2p} 4\pi a^2$$

### Direct Emulsion: ( $\varepsilon = a/R_{12}$ )

$$W_d = \frac{3\sigma_{12}V_1}{a} \varepsilon \{ (1 - \varphi_a b) + \varepsilon \varphi_a [f(\theta)(1 - \varphi_a b) - 2b \cos \theta] \}$$

### Reverse Emulsion:

$$W_r = \frac{3\sigma_{12}V_2}{a} \varepsilon \{ (1 - \varphi_a b) + \varepsilon \varphi_a [g(\theta)(1 - \varphi_a b) + 2b \cos \theta] \}$$

$\Delta W = W_d - W_r$  provides an Emulsification Criterion (which emulsion will form upon agitation):

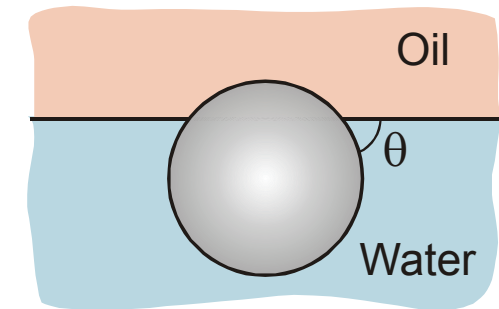
$\Delta W < 0 \Rightarrow$  the direct emulsion is formed;

$\Delta W > 0 \Rightarrow$  the reverse emulsion is formed.

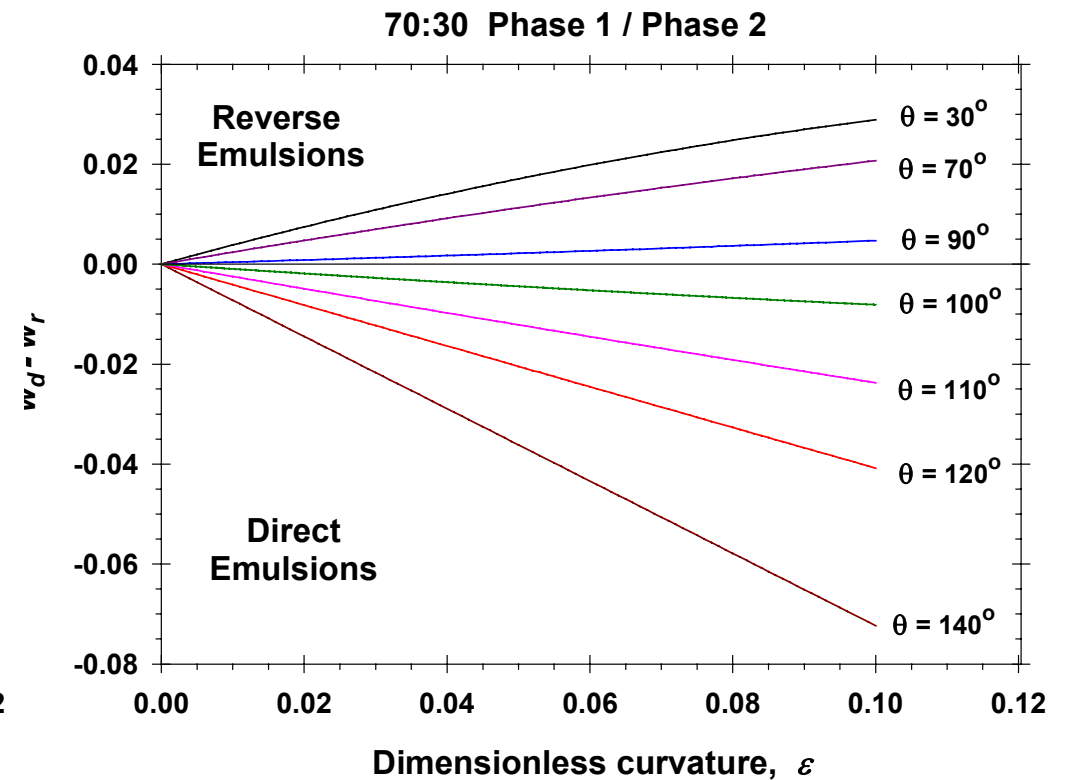
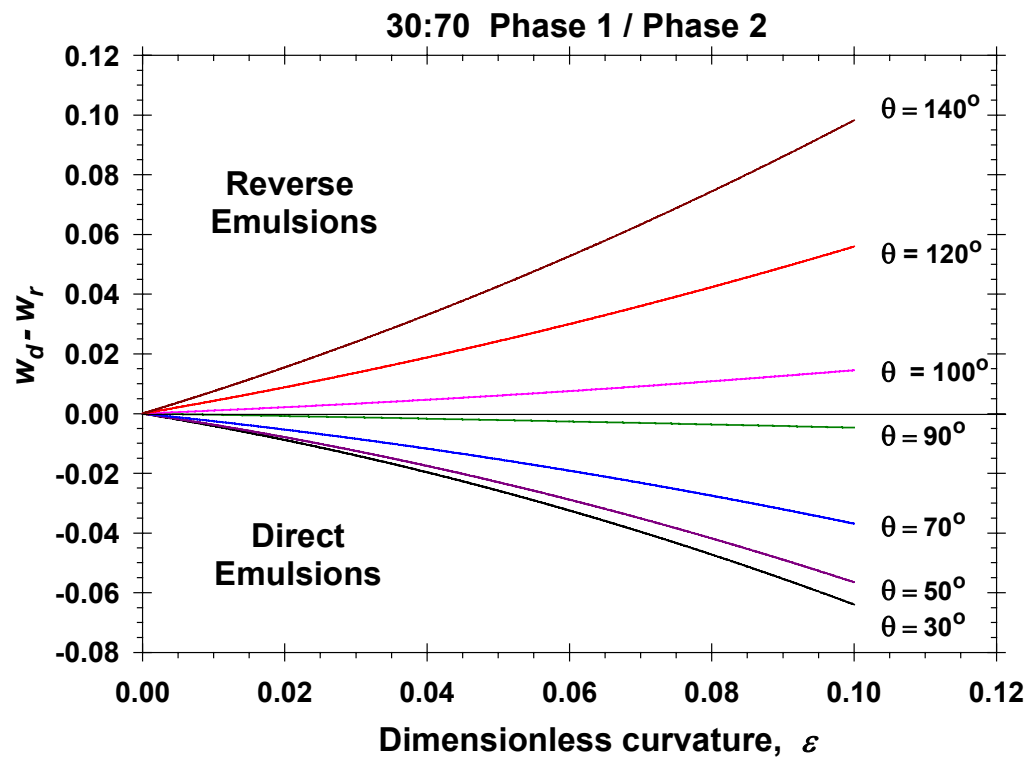
## Calculated Work of Emulsification:

$W_d - W_r < 0 \Rightarrow$  the direct emulsion is formed;

$W_d - W_r > 0 \Rightarrow$  the reverse emulsion is formed. ( $\varepsilon = a/R_{12}$ )



### Catastrophic phase inversion (?)



# Membrane Emulsification

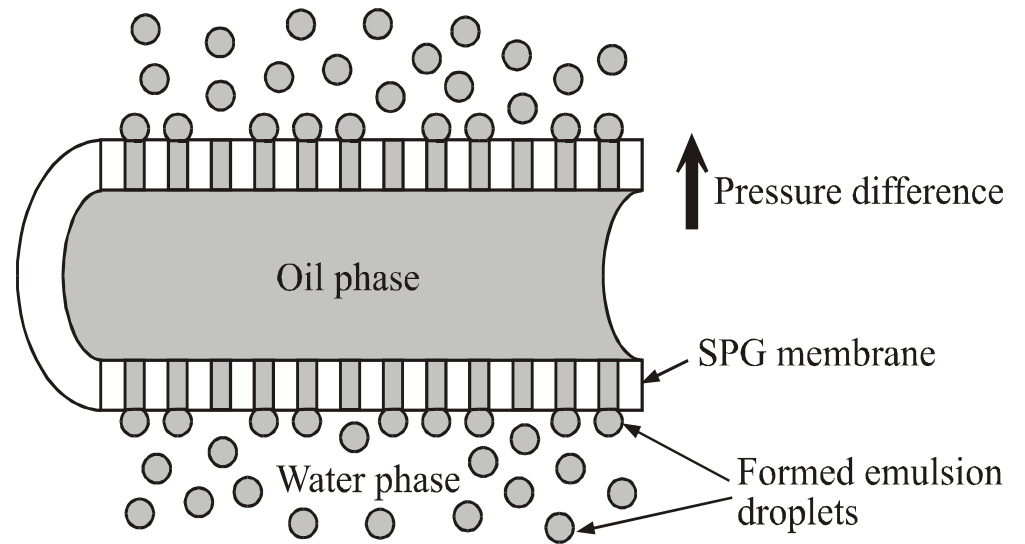
Porous **glass** or **ceramic** membrane

## New Task:

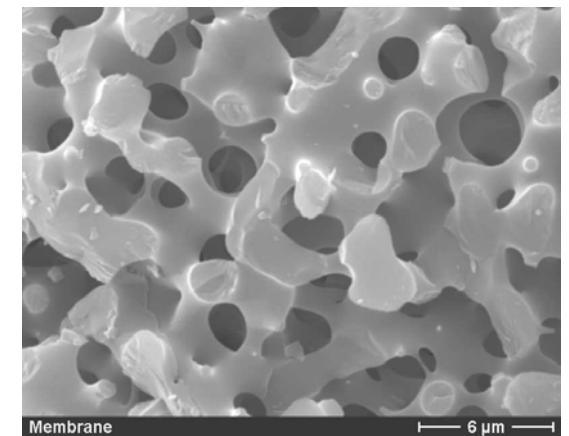
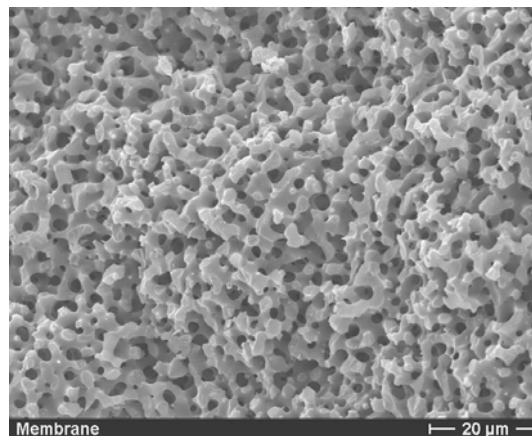
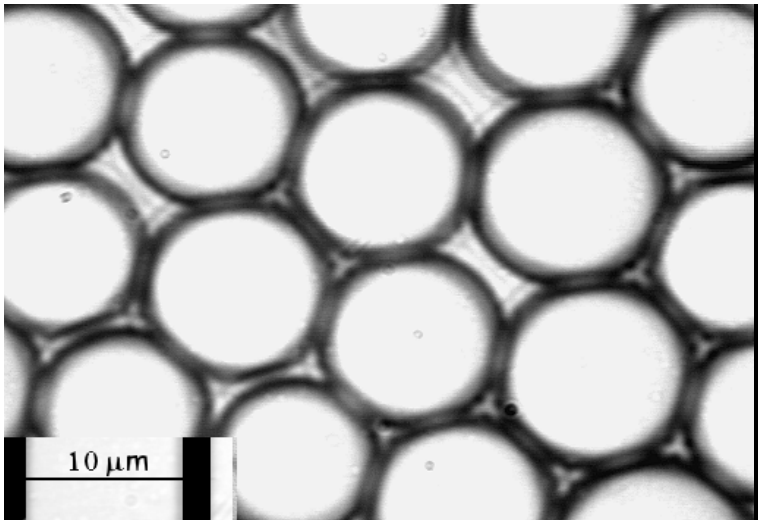
Apply this method to Pickering emulsions

Produced **monodisperse** common emulsion:

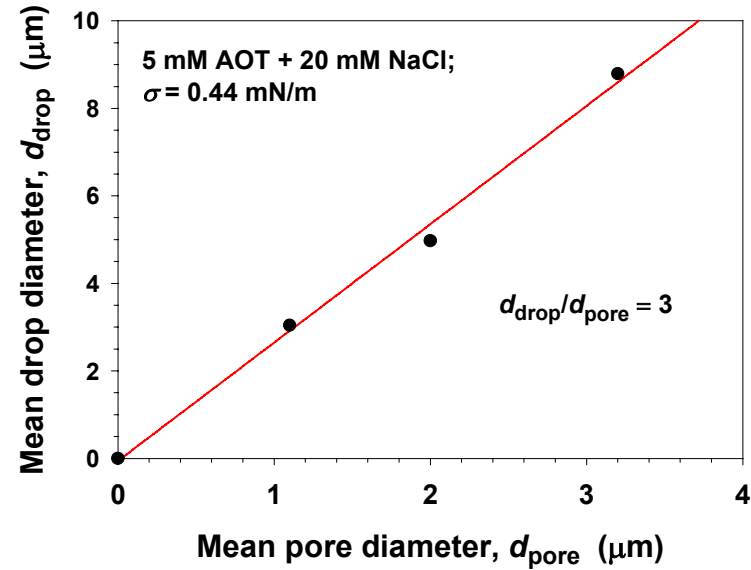
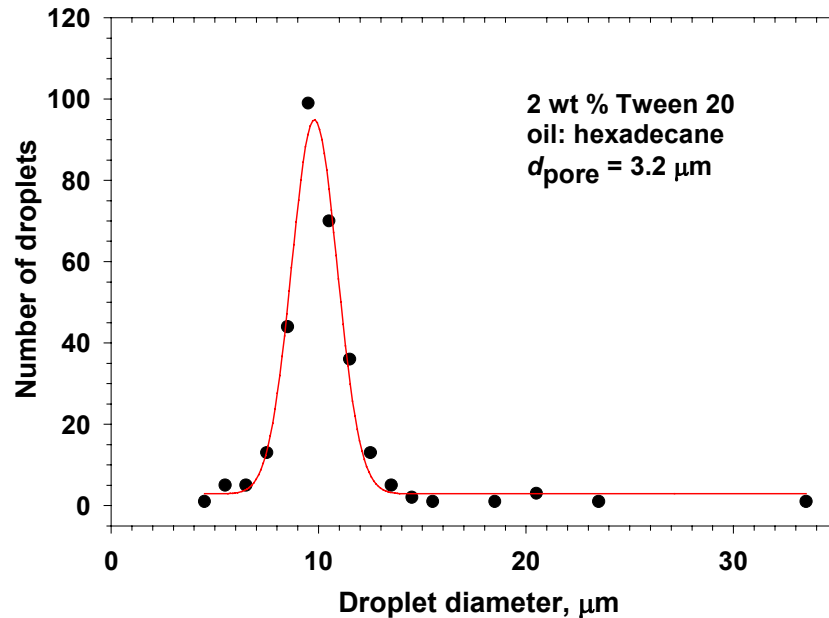
(pore diameter 3.2  $\mu\text{m}$ )



Surface of a membrane with **2  $\mu\text{m}$**  pore size



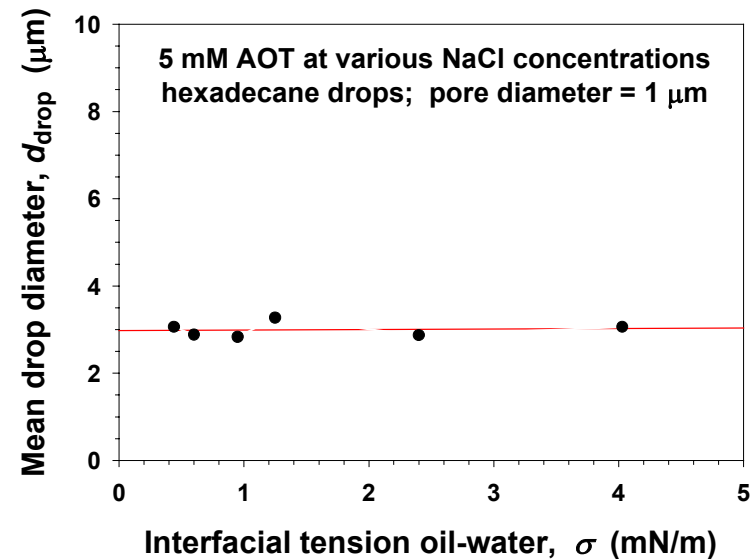
## Oil-in Water Emulsions Obtained by Hydrophilic Membranes



Typically  $d_{\text{drop}}/d_{\text{pore}} \approx 3$

$d_{\text{drop}}/d_{\text{pore}}$  is independent of the  
pore size

$d_{\text{drop}}/d_{\text{pore}}$  is independent of the  
interfacial tension



## **Basic Question:**

**Why  $d_{\text{drop}}/d_{\text{pore}} \approx 3$  ?**

**(irrespective of pore size, interfacial tension and viscosity of the liquid phases?)**

## **Theoretical Analysis:**

### **Condition for Detachment of a Growing Drop from a Pore**

## **KEY:**

**Analogy: detachment of a pendant drop**

- **Steady state growth:  $F_{\text{tot}} = 0$ ;**
- **At a given size the drop profile becomes unstable;**
- **The critical value of the body (gravitational) force is:**

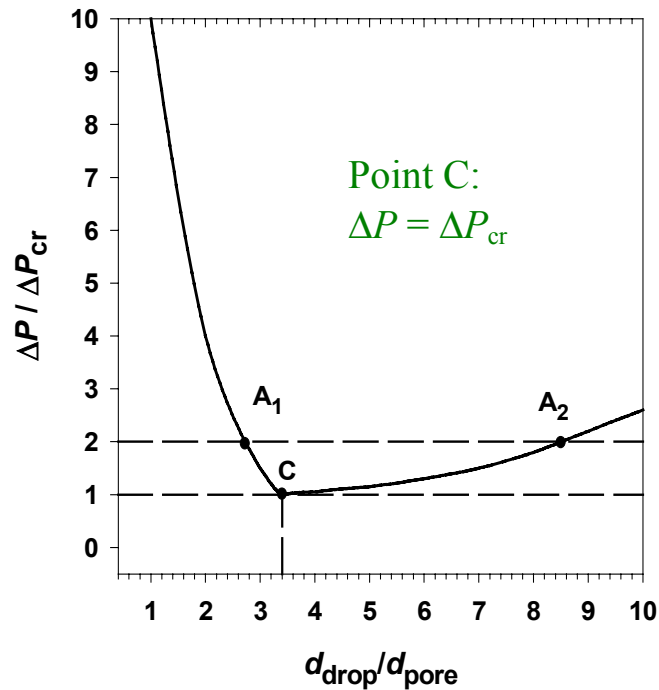
$$F_{\text{cr}} = \sigma d_{\text{drop}} \lambda(x)$$

$$x = d_{\text{drop}}/d_{\text{pore}}$$

$\lambda(x)$  – known universal function

$$\lambda(x) \propto (V_{\text{max}})^{2/3}; \quad V_{\text{max}} - \text{dimensionless maximum drop volume}$$

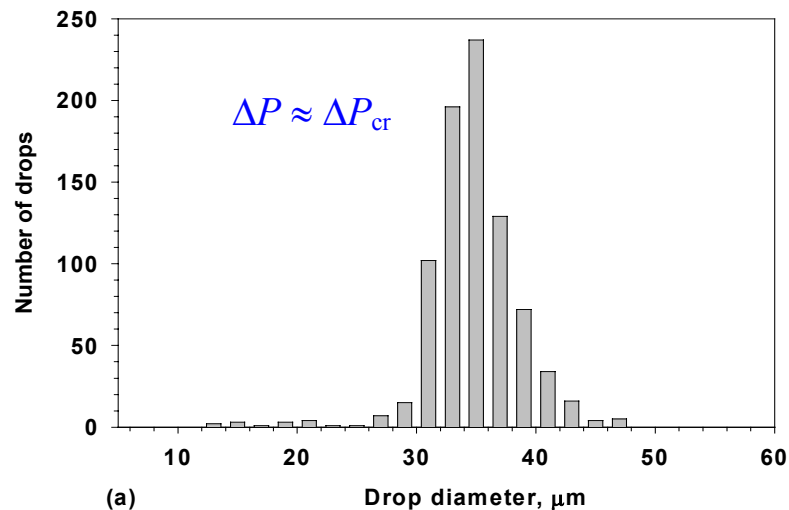




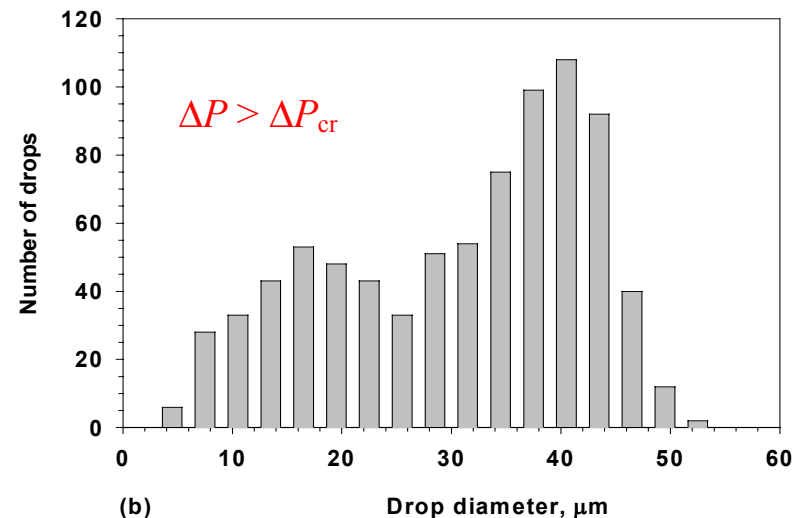
- For  $\Delta P < \Delta P_{cr}$  emulsion drops are not released from the membrane.
- For  $\Delta P > \Delta P_{cr}$  drops with two different sizes, corresponding to the points A<sub>1</sub> and A<sub>2</sub>,  $\Rightarrow$  two-peak drop-size distribution;
- For  $\Delta P = \Delta P_{cr}$  (point C) monodisperse drops are produced with  $d_{drop}/d_{pore} \approx 3$ .

$\Rightarrow d_{drop}/d_{pore} \approx 3$  (monodisperse drops), irrespective of the type of the oily and aqueous phases, interfacial tension, bulk viscosities, surfactant adsorption kinetics, etc.

$\Delta P = 0.02 \text{ kgf/cm}^2$ ; 0.25 M SDS + 12 mM NaCl,  
Pore diameter 10.4  $\mu\text{m}$ ; Oil: hexadecane



$\Delta P = 0.05 \text{ kgf/cm}^2$ ; 0.25 M SDS + 12 mM NaCl,  
Pore diameter 10.4  $\mu\text{m}$ ; Oil: hexadecane



## Summary of the New Tasks:

(1) Derive general expressions for **all types of capillary multipoles**;  
**rheology of particle monolayers**;

(2) Develop a **rigorous theory** of:  
(a) **electro-dipping force**;  
(b) lateral **capillary** and **electric** force.

(3) Investigate the **External-Meniscus driven capillary force**  
and its importance for the coalescence in **Pickering emulsions**

(4) Formulate a **thermodynamic criterion** for obtaining  
**direct/reverse Pickering emulsion** and check it against experiment

(5) Develop a **hydrodynamic** theory of **membrane emulsification** and  
apply this method to **produce experimentally Pickering emulsions**.

